11 - /1

ont nts o C pt rs n 4 r t r surt o or or t v r s r wt suprvsor tt w H nn ss - r r n r v rs ons o t s two pt rs v n pu rs s uss

## Con n

| 'n,            | o / on                                 | a       |
|----------------|--|---------|
| .1-1           | ru p ss n ro st                        | •       |
| 1-             | 0 r n                                  | <u></u> |
| 1-             | n qu po nt n u t on                    | _       |
| 1-4            | rv wot t ss                            |         |
|                | 141 ►r r qu s t s                      | .1      |
|                | o/brno/Bon                             |         |
| <del>-</del> 1 | o / . p n o / B on<br>r ns t on s st s | .11     |
| _              | D t o ns                               | .11     |
|                | orp seso trnu s                        | .1      |
|                |  | .1      |
|                |  | .1      |
| _              | r p s                                  | .1      |
|                | 1 orp s so s or r p s                  | .14     |
|                | rpstotrnstonsstrs                      | 1,      |
|                | rpsovr <sub>1</sub>                    | 1,1     |
| -4             | ru p ss n CC                           | .1-     |
| _              | B s ur t on                            | .1      |
| 4              | 1 For sFurton                          |         |
| _              | or rpswt ss n nt                       | 4       |

(n '

| n q x po n n on  1 A str t ons n FI                    |
|--|
| proo s st 1 4  |
| oun n ss n of pr t n ss or stron struct on             |
| - w s 11,<br>-4 Compret n ss or o s rv t on on ru n 11 |
| " 1m 0   |
| twor sor up r pro ss s 1                               |
| twor so r ur rpro ss s                                 |
|  |
| -1 up r 1 4  |

| •                          | o 🖍  |                      |
|----------------------------|--|----------------------|
| 1-1                        | C pt r p n n s   | .1                   |
| √1<br>-<br>-<br>- <b>4</b> | D nn t on r ton un tor  Err oprtonrs nt sorvru pssn CC  or oprtonrs nt so CC  t oprtonrs nt sorvru pssn CC                   | .1<br>.1<br>.1<br>.1 |
| _<br>_                     | In r n the s  In r n the s  In r n the s  A str top r tones that s  tt rn str top r tones that s  E p ns one ws or CB p r me | 4                    |
| <b>¬1</b><br>-<br>-        | Gr r ort ro  | F                    |
| - <b>4</b><br>- <u>3</u>   | F po nt run s  Int rpr t t on o rst or r po nt ro  s t onstru t on   | 3                    |
| -<br>-<br>-1<br>-1.1       | nrt prsrwrtnrrton  or ntrprttonso on ur  t onstruton ors or s nts  D ntono unton DApps ov ron ur  Frow r orpro ss            | 8                    |
| <b>3</b> –                 |  | 1 -                  |
| -4                         | nt tono Spec   | $\sqrt{1}$           |

p b \ ou

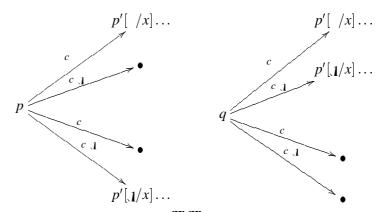
Commun ton n on urr n r t two un mit n on pts w r us to r o un rst n of pr n s st s-Arr s st n r rs s or t on o s n prts n us utono ous nts o out trus nss n p n ntr n sort nts tn on urr ntronot ors stors wr-Inprium; to ptur tun\_ vourot s st v w or st m - v or to ptt tt s sp to s st s n vom wm ntr ton or offun ton-sst stnto on urr n t or or pross rurus t t s v n r s to r r o o wor ov r t r s t w s-r s t t or o on urr n t ons r to t t or o r tr n ts l s ors ros s nrrstono uto t nw tons or vnts pro on urr ntrut w tws solows nt rott nto repprows n ppr ton ot strutur orr s stas nprt urrt osem opon nts ntr tn to orwor-s ons r tons w r to r on nr tr rs n t w ot stu o pro ss s— nr n p n ntr t or so pro ss s w r vrop roun t o of un tn nts p roun n to n vs r tons t r ur pr s nt n 1 1 1 r t rutso t ns v r s r nto pro ss s 1 1 1 4 1 1 or pr — s r ur prprov s nt t s r pt onso of un tn nts n nt so m pure on so t s r n u s of un ton s o r sorr s n rons ton so t tt t t t tur t trist troit on into not rs str t w - ss pr tr vr str ton ort ort rpurpos s ut or n sp tons on ws stort n rt n un I ntr sp ts o de un ton-For I pro on I ws to sr proto ors wr 

s ros r r r t to tr ns tons st s quot nt s ur ton qu v r n 1 - B s r r t s o n u t v r n n n proo s o qu v r n n n w th ss n s ur ton r r tons prov n r nt pro o o n u t v r son n - A sur o t su ss o s ur ton s t t tr ns tons st s n s ur ton qu v r n r now r so n us s on v n nt o r o n o n u t v proo t n qu or s qu nt r o put ton n t un ton r s tt n 1 1 1-

v n srnw tsr rr to s strong sturt on quvrn — r sn t u orsrnot on o sturt on quvrn m weak sturt on— stnus n proprt ow sturt on st to o un ton snoron rtr t snosrv r ton— In CC tsso not n t to o un ton pr trus n u so ortton sturt on tst tons nto ount n pstr o ntrnroput tonsw r sw sturt on tr tst ssunosrv r n strts rott — ons r sturt on squvrn s rus vr n t st ss n r r t r r to lor tr into t s nt so t stn quvrn orvrupssn r n u s—

vouros stes — r ppropret nesses storent rect to pture en nestru turo proses sweet serent entre nest to pture en nestru turo proses sweet en entre entre pero proses en entre e

us t the symbolic torpresent to t t sent topproto to t sopt nor reduce our rps-us vrus n vru pressons runntrpret nor rps nt some torunt tons or some to some topproto to some topprotorus to some topprotorus to some topprotorus topprotorus topprotorus topprotorus topprotorus topprotorus topprotorus states and no some symbolic nor some topprotorus states protorus topprotorus states protorus some sum some some species and some sum some some species and some sum some some species some sum some some species species some species specie



It sor r to sor to tot transitions stored or so pan q r nt rnot on o sur ton or viru pissin pro ssist ton ot ns v in ris non nto pur r n u s n optn r sor n motono s ur ton l ort r surt n tr ns ton s stars s me early saure ton l\_1-It s no surprise to the principle of the start of s r- r s n pt r rtrn tv ntono

s us su qust on pn surt tront of novrusus nt prss vt ot t prss ons rrow - rort s orp rt m n s urt ons o s or rps n 147 nt rt r surt t t v n r n u s o t

st tt tt wor sprintr wt rsp tto t of nst t in st tvr tons rrtv to t - rou outt t ssw wroo son rr us t tressoun nssor of prtnsswtoutt relative

Chapter 1. Introduction

t t r t ons us or n n r urs v pro ss s r un qu v ours— prop rt o s ur t on qu v r n w pro t s t t v n r r t on

$$X \Leftarrow= E$$

n two prosss p n q sutt p s so p represents E[p/X] n q s so p represents E[q/X] tn p n q ustt so p so p so p represents p using p so p represents p using p so p represents p under p so p represents p so p represents p represents p so p represents p

$$\frac{\vdash p = E[p/X]}{\vdash p = X}$$

w r  $X \Leftarrow= E$  s u r t s t u r n s s t t n s u r s t s o u n s s o t s r u r - A s u

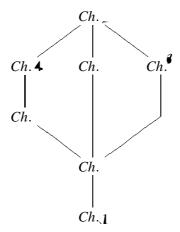


Figure 1.1. C pt r p n n s

ntu t v n r r s t on o t un qu po nt n u t on rur, w s rv r ro H n nss n ₄n.s propos run n us tortt r str ton on pr r trs-s ow rrtv of prtnsswtrsp tto stron stron or ur r urrpro sss-E tn n t swor urt rw oonto r trs o srv ton on ru n n s ov rt t t rrtrws u to mrl n n str us to str t roll nt mr t ons-A s uss on ont rrtons p tw npr trs ton n prmr o poston or vru pssnrnuss vnnw onrut ptrwtn proquvrn proo-

n t t s s w t s ort pt r st t n our on rus ons n v nu s or utur r sr -

v v q s ntons o transtons stys syurton nyru pss n Art ou wrvwt CC Fritwit pur pro ss rugwour stnt vnt nr n t st ssrrtrrtott toos 1.4.1 or oo ntrouton tot su t-Issus rrtn to vou pssns III ntsr pon num n no pror prn wt su on u ss r qu r - prop rt ro rst or r μ r urus pr s nt n C pt r s s on t ν o r  $\mu$  rucus u to o n n  $\rightarrow$ r tt 1 1 1 n qu nt n w

G v n two t r n u s  $D = (Var, \Sigma_V, I, Pr)$  n  $D' = (Var', \Sigma_{V'}, I', Pr')$  then s s ns to s w t p tw nt s ons sts o - row n o v r r n s so w v ton  $d_V Var \rightarrow Var'$  n w v n r t pr s rv n p  $d_\Sigma \Sigma_V \rightarrow \Sigma_{V'}$  not t t n  $\Sigma_{V'}$  r r ons r to  $\Sigma_V$  r r nt rpr t n  $f \in \Sigma_V$  s t nt rpr t t on o  $d_{\Sigma}(f)$  n  $\boldsymbol{A}$ 

Chapter 2. Symbolic Graphs and Symbolic Bisimulation 1

$$\frac{n \stackrel{b,\tau}{\longmapsto} n'}{[n,\delta] \stackrel{\tau}{\longrightarrow} [n',\delta]} \qquad \delta \models b$$

$$\frac{n \stackrel{b,c}{\longmapsto} n'}{[n,\delta] \stackrel{c}{\longrightarrow} [n',\delta]} \qquad \delta \models b,v = [\![e]\!] \delta$$

$$\frac{n \stackrel{b,c}{\longleftrightarrow} n'}{[n,\delta] \stackrel{c}{\longleftrightarrow} [n',\delta[v/x]]} \delta$$

$$\frac{\tau.p \xrightarrow{\tau} p}{c \ e.p \xrightarrow{c \ \llbracket e \rrbracket} p} \qquad \frac{\forall v \in Val}{c \ x.t \xrightarrow{c \ v} t[v/x]}$$

$$\frac{p \xrightarrow{\alpha} p'}{b \to p \xrightarrow{\alpha} p}$$

Chapter 2. Symbolic Graphs and Symbolic Bisimulation 1

**r**o ss s p

os ow  $p \sim q$  w wust n with n prittons n wovs or ot trinstons row ot p n q- sr t  $\nabla$  t sort trinston  $p \stackrel{,c}{\longmapsto} p'-$  tw rqur s prtton su t t or oor n b n t s p r t t on w now t t b u r n t s c x tr n s t on r o qto now strstbrrt to p' prttonwr qur t ns  $\{even(x), odd(x)\}$  – I w t even(x) w s t t $q \stackrel{c}{\longmapsto} q''$  w t  $p' \stackrel{even(x)}{\leadsto} q''$  n or odd(x) w us  $q \stackrel{c}{\longmapsto} q'$  w t p' = odd(x) q' - ourt r p r t t on n s r q u r n w not t t t oun v r r x o urs n t p r t t on n t s n r r t r t n r t s ur t on -

prvouse su st t ts 🗸 or s 🗸 un to nou tto prs rv on r ton — s ounts to s n t t

$$t = u$$
 pr  $s t \delta = u \delta$  or  $r \delta$ .

rrtons p two nonrt ns por spurtons n that tr-

**, opo** on 
$$t = b$$
 u if and only if  $t \delta = u \delta$  for all  $\delta \models b$ .

As ortown os wor rps st to retout rootwo men natern n pro ss s ntr t r r str n v ru p ss n pro ss s w r ntut v r n t n stru tur, ut r vo m n n t s vor r p s-For vpr, t pro ss X() r r

$$X \Leftarrow= \lambda x.c \ x.X(x+)$$

rpt routputst squn o vnnu rson c- strutur ot spro sssvrs pr trssnrstate roww trscoutput trnst on - turtrnst on rpw rso pp nsto t s pro r p ort s pro ss roo s r

$$X(\ ) \xrightarrow{c} X(\ ) \xrightarrow{c} X(\ 4) \xrightarrow{c} \cdots$$

Annnt rps nus to rortyrs prstrutur – n ppro tort ntsstutonwsprsnt npnntr nn ows - rwsrso skrrsorutonprsr nl usn rnt on rsk to s For rps-₁nn rows somuton nvorv ntroun prtss n nts or su st tut ons nto t  $\overline{r}$  so t  $\overline{r}$  ps  $\overline{r}$  us r us r vours su  $\overline{s}$  t  $\overline{v}$  pr  $\overline{X(\ )}$  n sr trtrnstons ron wt susttuton to sr owt tprtot pro ss s t transton s or rp wt ss m at or X() now roo sr

$$\bullet \xrightarrow{x = x + , c x} \begin{cases} x = x + , c x \\ x = x + , c x \end{cases}$$

or nrm s or rp wt ss n nts s or rp w os s r now r r wt trpr  $(b, \theta, \alpha)$  w r  $b \in BoolExp$   $\alpha \in Act$  n  $\theta$  s n ss n nt x = e $\text{wr t} \quad m \overset{b,\theta,\alpha}{\longmapsto} n \text{ to} \quad \text{not} \quad \text{r s o t} \quad \text{r p} \quad \text{n} \quad \text{s t} \quad \text{t} \ f v(b,e) \subseteq f v(m) \ \ f v(\alpha) \subseteq x \quad \text{n} \quad f v(n) \subseteq x \quad f v(n) \subseteq x \quad \text{n} \quad f v(n) \subseteq x \quad f v(n) \subseteq$ 

or rpswtss nent n unor ntos or rps n serre nn rto s tur tn s or rp w t su st tut ons—t rt n us n s pr su st tut ons ow v r w s tur t w t r trr su st tut ons— uş w n r t s or r p, rou r, t rur

$$\frac{m \overset{b,\theta,\alpha}{\longmapsto} n}{(m,\sigma) \overset{b\sigma,\alpha\theta\sigma}{\longmapsto} (n,\theta\sigma)}$$

s mows us to n s or s furton ov r r p s w t s s n n t s pr s n t t trrsptvs or rps swr r-An port nt tur o rps wt ss n nts st tn thor urr vru pss n

CC, t t s t surn u wtoutprmr of poston n r str ton s o m finite rst or rpr tro wtpr trs ponts—
In C ptr w prs nt proos st orr sonn outr unrvru pss n CC pro

ss s- on tus s or rpswt ss non t pr Itm rt ou on t

turn to t worr o ro stn s st s or our rst vonstr ton o t s or t n qu - r n u w ons r s CB, v ru p ss n pro ss r urus w r of un ton tw n nts s t t ro st n o v ru s - r n u s s r r n st r to v ru p ss n CC ut s v urt w s n ron s t on op r

| D s r   | Input  | <b>∮</b> utput                              |
|---|--|---|
| <u> </u>  |  |   |
| $\frac{w \not\in S}{x \in S \ t \xrightarrow{w} x \in S \ t}$                                     | $\frac{v \in S}{x \in S \ t \xrightarrow{v} t[v/x]}$                                     |   |
| $e \ p \xrightarrow{w} e \ p$   |  | $\frac{[[e]] = w}{e \ p \xrightarrow{w} p}$ |
| $\frac{\forall i \in I \cdot p_i \xrightarrow{w} p_i}{\sum_{I} p_i \xrightarrow{w} \sum_{I} p_i}$ | $\frac{\exists i \in I \cdot p_i \xrightarrow{\nu} p'}{\sum_I p_i \xrightarrow{\nu} p'}$ | $\exists i \in \S$                          |

E 
$$p = p$$
  $p = q$   $p = q$   $p = q$   $p = r$ 

AXIO 
$$\frac{p = q \in A \text{ of } s}{p = q}$$

Co G 
$$\frac{p_1 = q_1 p = q}{p_1 + p} = q_1 + q$$
 $\alpha$  Co 
$$\frac{x t = y t[y/x]}{x t = y t[y/x]} \quad y \notin fv(t)$$

$$\frac{\sum_{i \in I} \tau t_i[v/x] = \sum_{j \in J} \tau u_j[v/x] \text{ or } v \text{ r } v \in Val}{\sum_{i \in I} x t_i = \sum_{j \in J} x u_j}$$

$$\frac{p = q, [[e]] = [[e']]}{e p = e' q}$$

Bo 6 4 
$$\frac{[[b]] = \omega}{b \gg p = p} \quad \frac{[[b]] = \omega}{b \gg p = q}$$

Figure 3.2. In r n \_ tr s

$$v p + x v p \sim_n v p$$

or n pro  $ss \stackrel{\longleftarrow}{p-}$  of t tp s ros so x o s not o ur r r n vp n t r or n not t t utur v our o t t v p-In q s n pro ss w n s r i.e. q  $\longrightarrow$  t n

$$q + x \ q = n \ q$$

us q n s r n v ru − s n turn nst t

$$w(q+x q) \simeq_n w q$$
.

$$x t = x u \text{ row } t$$
 pot  $s s t = u$ 

E 
$$b \triangleright t = t$$
  $b \triangleright t = u$   $b \triangleright t = u$   $b \triangleright t = v$ 

$$C \stackrel{\triangleright t_1 = u_1 \quad b \triangleright t = u}{b \triangleright t_1 + t = u_1 + u}$$

s n t vo proos st vor op n t n s w now s ow t t t o s  $\mathcal{A}$  ron w t nor r s t on o o s v cl-Noisy to op n t n s prov soun n op r t o t s t on or stron no s on run ov r  $\mathcal{SA}$  n r r s t on o cl-Noisy s

Noisy 
$$e(t + x t) = e t$$
  $x \notin fv(t)$ 

w r t s t i o t or

$$\sum_{i\in I}b_i\gg e_i\;t_i.$$

of t t n ros nst nt tono su t n s r s v r tr ns tt v ru s n t n not r v n nput—Arrow n sr t us o not ton r t us n us  $\mathcal{A}_{\mathcal{N}}$  to r r to t o s  $\mathcal{A}_{\mathcal{N}}$  ron w t t n r r s o Noisy — rso wr t  $\mathcal{A}_{\mathcal{N}} \vdash b \rhd t = u$  to n t t  $b \rhd t = u$  n r v n t proo s st o F ur — ro t o s n  $\mathcal{A}_{\mathcal{N}}$ —

(Axiom Noisy is sound) For all  $\delta$ , if  $x \notin fv(t)$  then  $(e(t + x t))\delta \simeq_n (e t)\delta$ .

conser nor tree rose nest not to no Noisy  $w(p+xp) \simeq_n wp$  nor p st on p – It is suent to sow to the p+x p  $\sim_n p-$  to p to p and p is the sow to the p – It is suent to sow to the p – It is suent to sow to p – It is such that p – It is such that

00 As n 1411 w us ropost on - d to prov t tw n v r s no s s v or s v u rtont n

$$R \stackrel{def}{=} \left\{ (t\delta, u\delta) \mid \exists b \cdot \delta \models b \quad \mathbf{n} \quad (t, u) \in S^b \right\}$$

s nos spurton-prop w n v r R s nos spurtont n

$$S_{\mathcal{R}}^{b} \stackrel{def}{=} \{(t,u) \mid \delta \models b \ \mathbf{Fpr} \ \mathrm{s} \ (t\delta,u\delta) \in \mathcal{R}\}$$

ors nosson surtonr surt orrows sr roll t s- s our not r ttt proo otstor ns rt prssvnssot oor ntrnu - Es s nt m w r qur t powr to s r v n s ts o nv ron nts - s s s u s s u s s u s 

At propries on rights nor respect to the solution of the site of t w or t trnrssot oor nurs ont n wt n the-Frstr the tss to nstan ar or tsot of

$$\sum_{i \in I} b_i \gg e_i \ t_i + \sum_{i \in I_{\text{r-not}}}$$

s n CA E n ropos t on 
$$--$$
 w not  $n$  or  $K$ 

$$\vdash c_K \rhd t = \sum_K c_K \gg (\sum_{k \in K} \alpha_k . t_k).$$

 $v n t t \lor c_K = CA E v s$ 

$$\vdash \ \, \rhd t = \sum_{K} c_{K} \gg (\sum_{k \in K} \alpha_{k}.t_{k}).$$

It sorrt tt prottint sun n srsumtot strnson tons—
As n proowt utum rusv ursonom roms n usumwr r t r r to 1411 ropos t on - n not t tt proo t r n rso us to on ru t t

$$\begin{array}{ccc}
& b \triangleright \sum_{i \in I} c_i \gg \tau \ t_i = \sum_{j \in J} d_j \gg \tau \ u_j \\
& b \triangleright \sum_{i \in I} c_i \gg x \ t_i = \sum_{j \in J} d_j \gg x \ u_j
\end{array}$$

w r  $x \notin fv(b,c_i,d_j)$  s rv rur o t proo s st V-G v n st n r or  $t \equiv \sum_{i \in I} b_i \gg \alpha_i.t_i$  w not t t w n v oor n on tons to sr w nt n nputor s r – For nst n w now t tt oor n b w m u r nt t t t st rt tor v vru  $b \models \bigvee_I$ 

t or or nt CC this witrspittow shurton on run  $\approx_c$  1.4 p 1 reson shurtons p two nw shurton  $\approx$  n shurton on run  $\approx_c$  $p \approx q$ 

uppos t  $t u + x u \xrightarrow{d_j, e} u_{jl}$  n s or w us t t  $t t t \xrightarrow{b''} u$  to t v = v t n prt ton n vov – uppos t tu+x  $u\xrightarrow{d,x} u'$ –B ssur pt on d s  $d_j$  or –Cr rr d nnot  $d_j$  us sw v rr st rs  $u \stackrel{d_{j,x}}{\longrightarrow} u'$  us d ust n u' ust u-A n 

Chapter 3. Strong Bisimulation for CBS 4

rson t snr o

$$\boxed{Empty \quad x \in \emptyset \ X = \_ -}$$

now t t  $x \in I(q) - I(p)$   $p \xrightarrow{v} p$  w n v r  $v \in I(q) - I(p)$  o w r qu r  $q = q \xrightarrow{v} q'$  s  $v \in I(q)$  n  $v \notin I(p)$  so  $p \xrightarrow{v} p$  B us  $p \xrightarrow{u} q$  w t n now t t  $p \xrightarrow{u} q'$ 

ort us prt ur r $v\in S_l^j$  ns owt snnrr – nowt t $v\in S_l$  n $t_j[v/x]$   $au_n$   $u_l[v/x]$  – For onv nnr p,q not  $t_j[v/x]$ 

r r  $\blacksquare$  s no s ns to s w t  $I(\ ,t)$  s our - ppro w t s to r t r s t oor n pr ss ons b or w

of rwors  $b \wedge b' \models \neg b''_j$  or j-G v nt sw n ppr n u tonto o t n  $I(t\delta) = I(t_1\delta) = I(b \wedge b', t_1)$ -But sstsr pr pt -H n  $I(t\delta) = I(b, t) = \emptyset$ ow ust ons rt sw r K snon pt -B un or two ust v t tb  $\models b'$ sorrows us  $b_k$  n K so t or  $b' \wedge b''_k$  or so  $b''_k$ - In ts s b ust  $t_1$  un or n n u ton v s

| Ds r  | Input   | 🕯 utput  |
|---|---|--|
| , <i>Val</i>  |   |  |
| $x \in S \ t \ \stackrel{Val \setminus S}{\longmapsto} x \in S \ t$   | $x \in S \ t \xrightarrow{,x \in S} t$  |  |
| $e \ t \stackrel{,Val}{\longmapsto} e \ t$  |   | $e \ t \stackrel{,e}{\longmapsto} t$   |
| $ \frac{t \stackrel{b,S}{\longmapsto} t  u \stackrel{b',S'}{\longmapsto} u}{t + u \stackrel{b',b,S \cap S'}{\longmapsto} t + u} $ | $\frac{t \stackrel{b,x \in S}{\longmapsto} t'}{t + u \stackrel{b,x \in S}{\longmapsto} t'}$               | $\frac{t \stackrel{b,e}{\longmapsto} t'}{t + u \stackrel{b,e}{\longmapsto} t'}$              |
| $b' \gg t \xrightarrow{\neg b', Val} b' \gg t$  |   |  |
| $\frac{t \stackrel{b,S}{\longmapsto} t}{b' \gg t \stackrel{b,S}{\longmapsto} b' \gg t}$   | $ \frac{t \stackrel{b,x \in S}{\longmapsto} t'}{b' \gg t \stackrel{b' \land b,x \in S}{\longmapsto} t'} $ | $\frac{t \stackrel{b,e}{\longmapsto} t'}{b' \gg t \stackrel{b' \wedge b,e}{\longmapsto} t'}$ |

Figure 3.5. Tt rn str top r ton rs nt s

t tonson's onsrvtvon - tronstonsrrtonsr, s or r m wt oor n v r u s t n s u r s -  $r n s o ur n tr n s t on s o t on <math>b, x \in S$  now or t w t  $t p t t r n n p u t n \xrightarrow{b, S} w r S r or s t s t o v r u s w$  s r - b u r n twov stopr s ntt not on o patt rn no sy sy bo c b s u at on w t s nto ount t s to s t tt tx

 $t \stackrel{b_1,x \in S}{\longmapsto} t' \text{ t r} \quad \text{sts} \quad \text{v r} \quad r \quad z \text{ su} \quad \text{t} \quad \text{t} \quad z \not\in fv(b,t,u) \quad \text{n} \quad b \land b_1 \land z \in S \text{ p rt t on}$   $B \text{ su} \quad \text{t t or} \quad b' \in B \text{ t r} \quad \text{sts} \quad u \stackrel{b}{\longmapsto} u' \text{ su} \quad \text{t } \quad \text{t} \quad b' \models b \quad , \quad b' \models z \in S' \quad \text{n}$   $t'[z/x] \stackrel{b'}{\leadsto} u'[z/y]$ 

A n s u tr on t ons on u

**4-** 
$$S \neq \emptyset$$
,  $S' \neq \emptyset$ -
B or  $--t$  r sts  $t'$ ,  $u'$  su t t $t_i \rightleftharpoons_{pn}^{b''} t'$  n  $u_j \rightleftharpoons_{pn}^{b''} u'$  n  $d(t') < d(t)$ 

$$\begin{split} \operatorname{rtn} & S_K \stackrel{def}{=} \bigcap_{k \in K} (Val - S_k) \, \, r \, \operatorname{t} \\ & Exp(t \mid u) = \sum_{i \in I, j \in J} \quad (c_i \wedge d_j \wedge e_i \in S_j) \gg e_i \, (t_i \mid u_j [e_i / x]) \\ & + \sum_{i \in I, j \in J} \quad (c_i \wedge d_j \wedge e_j \in S_i) \gg e_j \, (t_i [e_j / x] \mid u_j) \\ & + \sum_{i \in I, K \subset J} \quad (c_i \wedge \bigwedge_{k \in K} \neg d_k \wedge e_i \in S_{J - K}) \gg e_i \, (t_i \mid u) \\ & + \sum_{j \in J, K \subset I} \quad (\bigwedge_{k \in K} \neg c_k \wedge d_j \wedge e_j \in S_{I - K}) \gg e_j \, (t \mid u_j) \\ & + \sum_{i \in I, j \in J} \quad (c_i \wedge \bigwedge_{k \in K} \neg d_k) \gg x \in S_i \cap S_j \, (t_i \mid u_j) \\ & + \sum_{i \in I, K \subset J} \quad (c_i \wedge \bigwedge_{k \in K} \neg d_k) \gg x \in (S_i \cap S_{J - K}) \, (t_i \mid u) \\ & + \sum_{j \in J, K \subset I} \quad (\bigwedge_{k \in K} \neg c_k \wedge d_j) \gg x \in (S_j \cap S_{I - K}) \, (t \mid u_j). \end{split}$$

Figure 3.6. E p ns on r ws or CB p r m r

of the provential of the provent of the properties of the provent of the provent

$$\langle - \rangle_{(f,g,\Lambda)} = -$$

$$\langle e \ t \rangle_{(f,g,\Lambda)} = f(e\Lambda) \ \langle t \rangle_{(f,g,\Lambda)}$$

$$\langle x \in S \ t \rangle_{(f,g,\Lambda)} = x \in g^{-1}(S) \ \langle t \rangle_{(f,g,\Lambda)}[g/x])$$

$$\langle b \gg t \rangle_{(f,g,\Lambda)} = b\Lambda \gg \langle t \rangle_{(f,g,\Lambda)}$$

$$\langle \sum_{i \in I} t_i \rangle_{(f,g,\Lambda)} = \sum_{i \in I} \langle t_i \rangle_{(f,g,\Lambda)}$$

$$\langle t_{(f',g')} \rangle_{(f,g,\Lambda)} = \langle t \rangle_{(f',f',g',g,\Lambda)}$$

r s to nsur t t n ro st tr ns ss on ro  $\langle t \rangle_{(f,g,\Lambda)}$  s tr ns t us n t un t on f- n pro ss  $p_{(f,g)}$  pp rs to r v v ru v w p t t ont nun pro ss to so t n o t on p'[v/x] ut w s t op r t on rs nt s F ur  $\neg 1$  t t t pro ss  $p_{(f,g)}$  w rst pp rn to r v v tu r r v s t v ru g(v) n ont nu s to v r p'[g(v)/x]- o ptur t s v our n t o n w n to r or us n t  $\Lambda$  un t on tr w tr ns t on g w s us w n x un oun n t n su s qu nt r us t t tr ns t on w r v r x o urs—

If 
$$\Lambda(x) = Id$$
 then  $\langle t \rangle_{(f,g,\Lambda[h/x])} \delta[v/x] \equiv \langle t \rangle_{(f,g,\Lambda)} \delta[h(v)/x]$ .

**100.** tru tur r n u t on on t-t nt r st n s s r w n t s pr t t uppos t s e t'-t n

$$\langle t \rangle_{(f,g,\Lambda[h/x])} \delta[v/x] \equiv f(e\Lambda[h/x]\delta[v/x]) \langle t$$

- $p \downarrow v$  t  $n q \stackrel{\varepsilon}{\Longrightarrow} q'$  or so q' su t  $t q' \downarrow v$
- $q \downarrow v t$   $n p \stackrel{\varepsilon}{\Longrightarrow} p'$  or so p'

$$\alpha.(X + \tau.Y) + \alpha.Y =_{ccs} \alpha.(X + \tau.Y) -$$

$$X + \tau.X =_{ccs} \tau.X -$$

n ortun to to vous vous vous ons of  $T_1$  in T or CB or not soun — vor some proof to the short in the solution of the short in the solution of the soluti

$$p \xrightarrow{w} p' \quad pr \quad s \quad p \xrightarrow{w} p' -$$

$$v \in I(p) \quad n \quad p \xrightarrow{v} p' \quad pr \quad s \quad p \xrightarrow{v} \stackrel{\varepsilon}{\Longrightarrow} p' -$$

$$v \in I(p) \quad n \quad p \xrightarrow{\tau \quad v} p' \quad pr \quad s \quad p \xrightarrow{v} p' -$$

s on tont  $t v \in I(p)$  n ss n sour rw nt ptt tw n prov p on runt to sturt v rs on o p-In or r to ot sw ust not intro u n n w nput tons nto t s tur t v rs on o p pur n v tons out roll n  $\tau$ ton— on t on  $v \in I(p)$  u r nt st t n nput ton ntro u w s r poss r—

For any standard form  $p \in SPA$ ,  $p \stackrel{w}{\Longrightarrow} q$  implies  $A_{P\tau} \vdash_{cl} p = p + w \ q$ .

**90.** B nutonont rnt ot rvton  $p \stackrel{w}{\Longrightarrow} q$ s s s str torw r I  $p \stackrel{w}{\longrightarrow} q$  t nw q s sum n o p us p s st n r -I Ppot n o + v s t proo  $\mathcal{A}_{P\tau} \vdash_{cl} p = p + w q$ uppos t t $p \xrightarrow{w} p' \stackrel{\tau}{\Longrightarrow} q$ - n n uw

$$\mathcal{A}_{\mathcal{P}\tau} \vdash_{cl} p = p + \tau \ (p' + x \in S \ q').$$

ow ow Tau3 wour ppr r  $S \subseteq I(p)$  ut w nnot nsur t s-How v r

• uppos t r sts  $p^{\tau}$  su t t  $p \xrightarrow{\tau} p^{\tau}$  n or q' su t t  $q \Longrightarrow q'$  w v  $p^{\tau} \not\approx q'$ -In t s s w s ow t t or s-

$$I(p+x \in S \ p) = I(p) \cup I(x \in S \ p)$$
  
=  $I(p) \cup (I(q) \setminus I(p)$ 

,00- ssspr ttro ntt of nrur ssoun wtrsp ttot

 $t \overset{b_{l},x \in S}{\longmapsto} t' \ t \quad r \qquad \text{sts} \quad \text{v} \ r \quad r \quad z \ \text{su} \quad t \quad t \ z \not\in fv(b,T,U) \quad n \qquad b \ \land$ 

2 B

p (D<sub>1</sub>,v on

A n w ssulp w tout ross o n r r t, t t t s st n r of - now t t  $t \stackrel{b', \tau \ S'}{\Longrightarrow} t'$  so suppos

$$t \stackrel{b_1,\tau}{\Longrightarrow} u \stackrel{b,S'}{\longmapsto} u \stackrel{b,\varepsilon}{\Longrightarrow} t'$$

w r  $b' = b_1 \wedge b \wedge b$  – uppos rso t t $u \equiv \sum_I b_i \gg x \in S_i \ u_i$  – n

$$b = \bigwedge_{j \in J} \neg b_j$$
 n  $S' = \bigcap_{j \in I \setminus J} (Val \setminus S_j)$ 

or sow s r n  $J \subseteq I$  - r t  $B_u = \{b \land b_K \mid K \subseteq I\}$  u un on b p rt t on n o s rv t t w n v r  $j \in K \cap J$  w v t t  $b \land b_K \models b_j$  n  $b \land b_K \models b \models \neg b_j \neg \neg$  n t s ontr post v r w v t t  $b \land b_K \neq \neg$  pr s  $K \cap J = \emptyset$  –

• ur nt nt on s to prov

$$\mathcal{A}_{\mathcal{P}\tau} \vdash b \land b_K \rhd \tau \ u = \tau \ (u + x \in S \ u)$$

ppr n of P-Noisy or AB D w n  $b \wedge b_K = \omega$  to u or  $b \wedge b_K$ -In or r to ot s w n to s ow t t  $S \cap I(b \wedge b_K, u) = \emptyset$  w n v r  $b \wedge b_K \neq \omega$ 

uppos t n t t  $b \land b_K \neq \infty$  n suppos or ontr t on t t  $v \in S \cap I(b \land b_K, u)$  — s ns t t  $v \in S$  n  $v \in S_j$  or so  $j \in K$ — But  $v \in S \subseteq S'$  pros t t  $v \in S' = \bigcap_{j \in I \setminus J} (Val \setminus S_j)$  t t s  $v \notin S_j$  or  $j \in I \setminus J$ — r or  $j \notin I \setminus J$  n w on ru t t j

 $b_u \in B_u$ or

otnt r surt us n *P-Noisy* n *Tau1* – Assult t n t t *S* s not pt – nnot ppr nuton to us to nt ptsot this snot rs -How vrt D oposton or 4-- vstrist" nu" su t td(t'') < d(t') d(u'') < d(u') $t'' \approx^{b''} t'$  n  $u'' \approx^{b''} u'$  t outross o n r r t w ssur t t  $d(t') \leq d(u')$  B n u t on t or ows t t  $\mathcal{A}_{\mathcal{P}\tau} \vdash b'' \rhd \tau \ t' = \tau \ t''$  w n  $\mathcal{A}_{\mathcal{P}\tau} \vdash b'' \rhd z \in S \ t' = z \in S \ t''$  — I — —It s r r

$$t' + x \in S$$
  $t'' \stackrel{\triangle}{=}^{b''} u' + x \in S'$   $u' + \tau u'$ 

n nutons ppr r r n

$$\mathcal{A}_{P\tau} \vdash b'' \rhd t' + x \in S \ t'' = u' + x \in S' \ u' + \tau \ u'.$$

s n t pr v ous r surt w n su st tut t' or t'' n ppr A n of P-Noisy to t  $\mathcal{A}_{\mathcal{P}\tau} \vdash b'' \rhd \tau \ t' = \tau \ (u' + x \in S' \ u' + \tau \ u').$ 

t r surt orrows s n t s w r S s pt - Appr t on o CA E n I pot n wr now r

$$\mathcal{A}_{P\tau} \vdash b_u \rhd \tau \ t' + \tau \ u' = \tau \ u'.$$

on run – s prov s CB w t pow r un qu t on nt or o o s rv t on on run – rt tt on run wons rws rv roll r sturtonsus nn m s nt s or CB w s to v n r t t r t s nt s nt r r - r or w n t s C pt r w t so out nts out r t s ur t ons n CB -

## A n / O CB

ons rw tt rts nts or CB t n ru t tt o not oo oput ton rs ns nt spr - r r ro C ptr t tt vov to rt s nt s nvorv r n up r pt on c  $x.t \xrightarrow{c} t[v/x]$  nto two p rts F rst w ons rt v ov

$$c \ x.t \xrightarrow{c} (x)t$$

str ton t ts un ton roll Val to

s nt s s not t m r r r son ort s s t t t of un t on proto or s r v n nts.'r tons to values nor – nt p n q r spon to t v ru 1 r v v n n srnrsptvr utt rspontot vru otr vn – pror r st tt rt s p nt s or p w nt to tr tt pt s pt s

$$p \stackrel{\{\underline{1}, \}}{\longrightarrow} (x \in \{\underline{1}, \})t,$$

w In s sn r t on roll q ut o ours q nnot prov sn r t on to t s tr ns t on—Fort sr son w ons rt with w r n vous o CB to unsut r to support rts nts n onotpursu ts ssu n urt rso on oprvtrston–Iw mtsprvtrzwwww vtorw  $vX.\langle a \ x\rangle(x=z+\ )\wedge X(x/z).$ nt n nst ntt t s po nt. sprvtrto v n

w r B s so or n on to non t v r r s t st no o s or r p n F s or ur o r st or r  $\mu$  r w us w t r t v r r s -

rustr toww nrest proosst retrewt torrown pro-Consr t point of un

$$A \equiv vX.\langle a \ x \rangle (x = z mod) \wedge X.(z \oplus 1)$$

w r A'' s sA' ut w t (z=1,t) rso n t t s t—1 n n w ppr rur u st us n t oor n z= — ot t t z=1  $\models$   $(z=[z\oplus 1/z])$  — sr s to t u n t z=  $\vdash$  t A''

$$F = B \mid F \lor F \mid F \land F \mid \langle \tau \rangle F \mid [\tau] F \mid \langle c \ x \rangle F \mid [c \ x] F \mid \langle c \ \rangle G \mid [c \ ] G \mid A.(e/x)$$

$$G = \exists x. F \mid \forall x. F$$

$$A = X \mid vX[\mathcal{A}] F \mid \mu X[\mathcal{A}] F$$

Figure 5.1. Gr r ort ro

In soft toro to rotter wr Grn sovrquat or ur- to roprtors  $\langle c x \rangle$  n [c x] ts n rs ort vr r x s ot qunt rs  $\exists x$  n  $\forall x$  wrt fv(F) ort r tvr rso F - snoton s r r or on F wr w tout points - F n r Arn sovr fixpoint abstractions ut t s one us to n or or or ur t onstru t on A.(e/x) — s not s t ppr t on o t str t on A to t su st tut on [e/x] s onstruton n s mot r t v r r so x n A t us w v t t

$$fv(A.(e/x)) = fv(e) \cup (fv(A) \setminus \{x\})$$

w r fv(e) s v n t t v(A) s n

$$fv(vX[\mathcal{A}]F) = fv(\mu X[\mathcal{A}]F) = fv(\mathcal{A}) \cup fv(F)$$
 n  $fv(X) = \emptyset$ .

ntono  $fv(\mathcal{A})$  stovous on -A on ur F some recursion closed FV(F) s Fig. 1. The pt. in s. in data closed fv(F) is Fig. 1. A so t. on  $vX[\mathcal{A}]F$  or  $\mu X[\mathcal{A}]$ 

on propos n 14 ] w r t s s own to r t r st or r t s writing qu v r n - s t t t po nts prov no tr st n u s n pow r ov r pro ss s-

**, opo** on  $t \sim_L^b u$  if and only if for all recursion closed formulae F with empty tag sets,

$$t \models_b F iff u \models_b F$$

uppos  $\delta \models b$  in r t p,q not  $[t,\delta]$  in  $[u,\delta]$  risplies r to r to significant r us in the original suppose p = Lu = 0 in the second r upposes p = Lu = 0 in the second r upposes p = Lu = 0 in the second r upposes r in the second r in the

$$\begin{array}{lcl} [\![\mu\ X.F]\!]\rho\delta & = & \emptyset \\ [\![\mu^{\alpha+,1}\!X.F]\!]\rho\delta & = & [\![F[\mu^{\alpha}\!X.F/X]]\!]\rho\delta \\ [\![\mu^{\gamma}\!X.F]\!]\rho\delta & = & \bigcup_{\alpha<} \end{array}$$

$$Id \frac{B \vdash t \mid B}{B \vdash t \mid B} \qquad Case \frac{B_{\downarrow} \vdash t \mid F, \dots, B_{n} \vdash t \mid F}{\bigvee_{\downarrow, \leq i \leq n} B_{i} \vdash t \mid F}$$

$$Cons \frac{B_{\downarrow} \vdash t \mid F}{B \vdash t \mid F} \quad (B \models B_{\downarrow}) \qquad Ex \frac{B \vdash t \mid F}{\exists x.B \vdash t \mid F} \quad (x \notin fv(t, F))$$

$$\alpha \frac{B \vdash t' \mid F'}{B \vdash t \mid F} \quad (t' \equiv t, F' \equiv F) \qquad \wedge \frac{B \vdash t \mid F_{\downarrow} \mid B \vdash t \mid F}{B \vdash t \mid F_{\downarrow} \land F}$$

$$\forall_{L} \frac{B \vdash t \mid F_{\downarrow}}{B \vdash t \mid F_{\downarrow} \lor F} \qquad \forall_{R} \frac{B \vdash t \mid F}{B \vdash t \mid F_{\downarrow} \lor F}$$

$$\langle \tau \rangle \frac{B \vdash t' \mid F}{B \land b \vdash t \mid \langle \tau \rangle F} \quad t \stackrel{b, \tau}{\mapsto} t'$$

$$\exists T \mid \frac{B \land b_{\downarrow} \vdash t_{\downarrow}}{B \land b \vdash t \mid \langle \tau \rangle F} \quad t \stackrel{b, \tau}{\mapsto} t'$$

$$\langle c \mid \frac{B \vdash t' \mid F[e/x]}{B \land b \vdash t \mid \langle c \mid x \rangle F} \quad t \stackrel{b, c \mid e}{\mapsto} t'$$

$$[c \mid \frac{B \land b_{\downarrow} \vdash t_{\downarrow}}{B \land b \vdash t \mid \langle c \mid x \rangle F} \quad t \stackrel{b, c \mid e}{\mapsto} t'$$

$$w \mid \{(b_{\downarrow}, t_{\downarrow}, e_{\downarrow}), \dots, (b_{n}, t_{n}, e_{n})\} = \{(b, t', e) \mid t \stackrel{b, c \mid e}{\mapsto} t'\}$$

 $\langle c \rangle \xrightarrow{B \vdash (y)t' G} (t \xrightarrow{b,c} (y)t')$ 

 $[c] \quad B \wedge b_1 \vdash (y_1)t_1 \quad F, \ldots, B$ 

u st  $B \vdash t \quad A.(z/z)$ 

$$ts tB = B$$
  
 $ts tF_1 \wedge F = ts tF_1 \wedge ts tF$ 

$$ts tF_1 \vee$$

 $s t - s \alpha$  onversion pr  $s two ror s nt s on struction restrictions <math>s t - s \alpha$  on  $s - s \alpha$  on

o urnt stutonwrt t sto  $A_j$  decreases ns pssn row on ur  $F_n$  to  $F_{n+1}$  sowt tt one w ts n ppns  $A_i \square A_j$ 

sss to treat to stors — ntrount on well pointers—point rs r sin soft to  $A_j$  in  $F_n \in \mathcal{C}$  points to soft  $A_{j'}$  to  $F_{n'}$  in C' or to soft  $A_{j'}$  in  $F_n$  — non the point rs soft to  $F_n$  in  $F_n$  point to the semistration of  $F_n$  in the semistration of  $F_n$  in the semistration of  $F_n$  in the semistration of  $F_n$  is point rs, then the semistration of  $F_n$  in the semistration of  $F_n$  is point rs, then the semistration of  $F_n$  in the semistration of  $F_n$  is point rs, then the semistration of  $F_n$  in the semistration of  $F_n$  in the semistration of  $F_n$  is point to  $F_n$ . Then, and the semistration of  $F_n$  is the semistration of  $F_n$  in the semistration

sul nour proof we suppose to not seen point residue to the norm of the sequence of the sequen

s prov s t t $A_i \sqsubseteq A_j$  w n v r  $v_{n+1}^j > v_n^j$ —But toporo r sort n t rs us t t i < j t us  $v_{n+1} < v_n$  n t r o r p or r n on v tors us  $v_{n+1}^i < v_n^i$ — s s tru or n so w v n n n t s n n n o v tors w t r sp t t

Chapter 5. Local Model Checking for Value-Passing Processes

```
(t,F_1 \wedge F) \mapsto (t,F_1) n
                                                                             (t,F_1 \wedge F) \implies (t,F)
                                                                              (t,F_1 \vee F) \mapsto (t,F)
(t,F_1 \lor F) \mapsto (t,F_1)
(t,\langle \mathsf{\tau} \rangle F \qquad \rightarrowtail \quad (t',F) \qquad \quad \text{or}
                                                                              t \stackrel{b,\tau}{\longmapsto} t'
                                                                               t \xrightarrow{b,\tau} t'
(t,[\tau]F) \longrightarrow (t',F) or
                                                                               t \stackrel{b,c}{\longmapsto} t'
(t, \langle c x \rangle F \longrightarrow (t', F[e/x]) or
                                                                               t \stackrel{b,c}{\longmapsto} t'
(t, [c \ x]F) \longrightarrow (t', F[e/x]) or
                                                                               t \stackrel{b,c}{\longmapsto} t'
(t,\langle c \rangle G) \longrightarrow ((x)t',G)
                                                               or
                                                                           t \stackrel{b,c}{\longmapsto} t'
(t, [c \ ]G) \longrightarrow ((x)t', G)
                                                               or
\begin{array}{lll} ((x)t, \forall y.F) & \rightarrowtail & (t[w/x], F[w/y]) & \text{w} & \text{r} & w = new(fv((x)t, \forall y.F)) \\ ((x)t, \exists y.F) & \rightarrowtail & (t[w/x], F[w/y]) & \text{w} & \text{r} & w = new(fv((x)t, \forall y.F)) \end{array}
(t,A.(e/z)) \rightarrow (t,A)
(t, \mathsf{V} X[\mathcal{A}] F) \ \longmapsto \ (t, F[\mathsf{V} X[\mathcal{A}^+] F/X]) \quad t \not\in \mathcal{A}
```

w r  $\mathcal{A}^+ = \mathcal{A} \cup (t \operatorname{s} \operatorname{tv} X[\mathcal{A}]F, t)$ 

Figure 5.7. nrt prsrwrtnrrton

p p For finite G and pairs (t,F) generated from (t,F) with  $\eta$  as above:

 $[[t sat F]] \eta \vdash t F.$ 

rt prs- on s s o ntrst r r ppr ton n ponton ur o n t t s to t point of  $VX[\mathcal{A}]F$  t n run V n t n to no  $\eta$  V s t T suct it rws, nutonw nowt t

 $[t s tF[vX[\mathcal{A}']F/X]]]\eta \vdash t F[vX[\mathcal{A}']F/X]$ 

 $w \quad r \quad \mathcal{A}' = \mathcal{A} \cup (t \text{ s } \text{ tv} X[\mathcal{A}]F, t) - \text{But } \llbracket t \text{ s } \text{ t} F[\text{v} X[\mathcal{A}']F/X] \rrbracket \eta \quad \text{s} \quad \text{s } \text{r} \quad \text{s} \quad \text{n to} \quad \llbracket t \text{ s } \text{ tv} X[\mathcal{A}]F \rrbracket \eta$ so run  $V_1$  w v our r surt-I F s t our A.(e/z) t n n u t on t rms us tnn

(Completeness) For all formulae F with empty tag sets, finite G,  $fv(B) \subseteq fv(t)$ ,  $t \models_B F implies B \vdash t F$ .

r n rotsstons vot to strsnts-snnws nt s t symbolic semantics or to to tour of protoness r surt - As for ntrpr t ton t s r urs on nv rong nt n oog n pr ss on r t r t n t nv rong nt n or r to ntrprtt r t v r rs- oor n r pr s nts t s to r t nv rom nts w sts t-Itwo us unto nt nt rou out of prtn ssproo vr str to or or t s oor n pr ss ons- ssult t t v t on

$$B \wedge (z = e)$$

w r B s oor n pr ss on not ont n n n r urs on p r  $\P$  t rs n e s n t v tor o t pr ss ons rso not ont n n n r urs on p r trs- For not t on r onv n n w sr su oor n s orrows- tern ovrsusttutons o t on

Cs F point ppro tons—sowt s F s  $\mu^{\alpha}X.F'$ —uppos  $t \models_{B\hat{\epsilon}} \mu^{\alpha}X.\theta F'$ —I  $\alpha$  s t in  $H(\theta F)$  or striving  $H(\mu^{\beta}X.F')$  or s or  $m\beta < \alpha$ 

```
\varepsilon \triangleright t s tB = B[\varepsilon(z)/z]
                  \varepsilon \triangleright t s \ tF_1 \wedge F = \varepsilon \triangleright t s \ tF_1 \wedge \varepsilon \triangleright t s \ tF
                  \varepsilon \triangleright t s \ tF_1 \vee F = \varepsilon \triangleright t s \ tF_1 \vee \varepsilon \triangleright t s \ tF
                  \varepsilon \triangleright t \operatorname{s} \operatorname{t} \langle \tau \rangle F = \bigvee b' \wedge \varepsilon \triangleright t' \operatorname{s} \operatorname{t} F
                                                                                          t \stackrel{b',\tau}{\longrightarrow} t'
                 \varepsilon \triangleright t \operatorname{s} t[\tau]F \qquad = \bigwedge_{t \stackrel{b',\tau}{\longrightarrow} t'} b' \rightarrow \varepsilon \triangleright t' \operatorname{s} tF
                  \varepsilon \triangleright t \operatorname{s} \operatorname{t} \langle c x \rangle F = \bigvee b' \wedge \varepsilon \triangleright t' \operatorname{s} \operatorname{t} F[e/x]
                                                                                           t \xrightarrow{b',c} e t'
                  \varepsilon \triangleright t \operatorname{st}[c \ x]F \qquad = \bigwedge_{\substack{t^{b',c}e'\\t' \mapsto t'}} b' \to \varepsilon \triangleright t' \operatorname{st}F[e/x]
                 \varepsilon \triangleright t \operatorname{s} \operatorname{t} \langle c \rangle G = \bigvee_{t \stackrel{b',c}{\longmapsto} (x)t'} b' \wedge \varepsilon \triangleright (x)t' \operatorname{s} \operatorname{t} G
                  \varepsilon \triangleright t \operatorname{st}[c]G = \bigwedge_{t \stackrel{b',c}{\leftarrow}(x)t'} b' \rightarrow \varepsilon \triangleright (x)t' \operatorname{st}G
                  \varepsilon \triangleright (y)ts \ t \forall x.F = \forall w.(\varepsilon \triangleright t[w/y]s \ tF[w/x]) \ w = new((y)t,\varepsilon,\forall x.F)
                  \varepsilon \triangleright (y)ts \ t\exists x.F = \exists w.(\varepsilon \triangleright t[w/y]s \ tF[w/x]) \ w = new((y)t, \varepsilon, \exists x.F)
                  \varepsilon \triangleright t \operatorname{st} A.(e/z) = [\varepsilon(e)/z] \triangleright t \operatorname{st} A
                \varepsilon \triangleright t \operatorname{st} VX[\mathcal{A}]F = \begin{cases} \lfloor B \rfloor & \exists (B\widehat{\varepsilon}', t) \in \mathcal{A} \operatorname{wt} B\widehat{\varepsilon}' \models \widehat{\varepsilon} \\ VX_{t\varepsilon} \cdot (\varepsilon \triangleright t \operatorname{st} F[VX[\mathcal{A}^+]F/X]) & \operatorname{ot} \operatorname{rw} \operatorname{s} \end{cases}
\varepsilon \triangleright t \operatorname{st} \mu X[\mathcal{A}]F = \begin{cases} \varepsilon & \exists (B\widehat{\varepsilon}', t) \in \mathcal{A} \operatorname{wt} B\widehat{\varepsilon}' \models \widehat{\varepsilon} \\ (\varepsilon \triangleright t \operatorname{st} F[\mu X[\mathcal{A}^{+\mu}]F/X]) & \operatorname{ot} \operatorname{rw} \operatorname{s} \end{cases}
w r \mathcal{A}^+ = \mathcal{A} \cup ((\varepsilon \triangleright t s \ t \lor X[\mathcal{A}]F)\widehat{\varepsilon}, t) n \mathcal{A}^{+\mu} = \mathcal{A} \cup ((\varepsilon \triangleright t s \ t \mu X[\mathcal{A}]F)\widehat{\varepsilon}, t)
                                                                                 Figure 5.9. to nstrut on or s or s nt s
```

$$\begin{array}{ccc} DApps(B) & = & DApps(X) & = & \emptyset \\ DApps(F_1 \wedge F) & = & DApps(F_1 \vee \\ \end{array}$$

Chapter 5. Local Model Checking for Value-Passing Processes

n us n  $\mu$  un or n s n  $[\tau]$  rur s n [i] rur - ow ot - n -4 n r u to t s n r u  $\widehat{\epsilon}$  ht  $\widehat{\epsilon}$  ht  $F[\tau]$ 

sounnssot proot nqu FI or sprnpmutot onutv nton o s rt -Cons rt two nts

$$X \Leftarrow= \alpha.X$$
 n  $Y \Leftarrow= \alpha.Y + \alpha.X$ .

wour ppr onv n ours rv st tX n Y r s r r son n s r rtot r son n w wour us or FI- wour ons r α ov roll Y n t twt vov roll Y r s  $\mathbb{Z}^n$  r-Form  $\mathbb{Z}^n$  w wown onstru t  $\mathcal{R}=\{(X,Y),(X,X)\}$  s  $\mathbb{Z}^n$  w to ss  $\mathbb{Z}^n$  on nt npp rtot onutonprnprw tresust t $\mathcal{R}\subseteq$  ---

Firm us n um rton  $\{X_i \Longleftarrow p_i\}_I$  s s  $\Gamma$ rnsprttot prvous run – simultaneously st rs t pot s st t

$$\vdash q_i = p_i[q/X]$$

ort i s  $\{q_i\}_I$  n ur r tons  $\{p_i\}_I$ -Froi t sw n rt t $q_A = X_I$ purpos o t s ptr s to nv st t t us o un qu po nt n u ton n v ru pssn rnu nor rto r trs structon quvrn sovr rsso r ursvr n nts-prt urrenu w ons rsvrupssnCC utw nt pttt t sussonwm ppm m to w mmsso pro ssmn u s nmu n CB –

w r  $f_i \equiv \lambda x_i.u_i$  n  $\{X_i \Longleftarrow \lambda x_i.t_i\}$  s u r r t on— s rur, n v r st t s ov, s unsoun —H nn ss n  $\{x_i, t_i\}$  prov t or ow n  $\{x_i, t_i\}$  prov t or ow n  $\{x_i, t_i\}$  prov t  $\{x_i, t_i\}$  prov t or ow n  $\{x_i, t_i\}$  prov t or ow n  $\{x_i, t_i\}$  prov t or over  $\{x_i, t_i\}$  prov t

How v r t r r t on s n r pr tr on s qu nt n or r to row r r t ons to t n r proo -For r pr suppos proo w r tt r pt n r s to t su o r

$$\vdash_D b \rhd t = u$$

w r t n u r ot n  $\mathcal{T}_{D^-}$  on v r  $\blacksquare$  t v to ntro u n w nt onst nt Xt n n D

E 
$$\frac{| -b | b | t | - u}{| -b | b | b | t | t} = \frac{| -b | b | t | t}{| -b | b | b | t | t}$$

$$\frac{| -b | b | t | t}{| -b | b | t | t} = \frac{| -b | b | t | t}{| -b | b | t | t}$$

$$\frac{| -b | b | t | t}{| -b | b | t | t} = \frac{| -b | b | t | t}{| -b | b | t}$$

$$\frac{| -b | b | t | t}{| -b | b | t} = \frac{| -b | b | t | t}{| -b | b | t}$$

$$\frac{| -b | b | t | t}{| -b | b | t} = \frac{| -b | b | t | t}{| -b | b | t}$$

$$\frac{| -b | b | t | t}{| -b | b | t} = \frac{| -b | b | t | t}{| -b | b | t}$$

$$\frac{| -b | b | t | t}{| -b | b | t} = \frac{| -b | b | t | t}{| -b | b | t}$$

$$\frac{| -b | b | t | t}{| -b | b | t} = \frac{| -b | b | t | t}{| -b | b | t}$$

$$\frac{| -b | b | t | t}{| -b | b | t} = \frac{| -b | b | t | t}{| -b | b | t}$$

$$\frac{| -b | b | t | t}{| -b | b | t} = \frac{| -b | b | t | t}{| -b | b | t}$$

$$\frac{| -b | b | t | t}{| -b | b | t} = \frac{| -b | b | t | t}{| -b | b | t}$$

$$\frac{| -b | b | t | t}{| -b | b | t} = \frac{| -b | b | t | t}{| -b | b | t}$$

$$\frac{| -b | b | t | t}{| -b | b | t} = \frac{| -b | b | t | t}{| -b | b | t}$$

$$\frac{| -b | b | t | t}{| -b | b | t} = \frac{| -b | b | t}{| -b | b | t}$$

$$\frac{| -b | b | t | t}{| -b | b | t} = \frac{| -b | b | t}{| -b | b | t}$$

$$\frac{| -b | b | t | t}{| -b | b | t}$$

$$I \qquad \frac{\vdash_D b \rhd t = u}{\vdash_{D \cup E} b \rhd t = u}$$

$$E \qquad \frac{\vdash_{D \cup E} b \rhd t = u}{\vdash_{D} b \rhd t = u} \qquad t, u \in \mathcal{T}_{D}$$

FI 
$$\frac{\forall i \in I \quad \vdash_D \quad \triangleright g_i = f_i[g/X]}{\vdash_{D \cup E} \quad \triangleright g_1 = X_1} \quad \text{w} \quad \text{r} \quad E = \{X_i \Longleftarrow f_i\}_I$$
s u r r t on

$$\lambda I$$
  $\frac{\vdash_D b \rhd f(x) = g(x)}{\vdash_D b \rhd f = g}$   $x \not\in fv(b)$   $n \ x_i \neq x_j \text{ or } i \neq j$ 

$$\lambda \to \frac{\vdash_D b \rhd f = g}{\vdash_D b \rhd f(e) = g(e')} \quad b \models e = e'$$

$$\beta \qquad \qquad \overline{\vdash_D \quad \rhd (\lambda x.t)(e) = t[e/x]} \qquad \qquad x$$

Figure 6.2.

onv rs o t s s t nt r st n propos t on o of pr

Let  $D_1 = \{X_i \iff f_i\}_I$  and  $D = \{Y_j \iff g_j\}_J$  be standard declarations such that  $X_1(e_1) \implies_L Y_1(e_1')$ . Then there exists a standard declaration  $E = \{Z_{ij} \iff h_{ij}\}_{I \times J}$  such that

$$\mathcal{A} \vdash_{D_1 \cup E} b \rhd X_1(e_1) = Z_{11}(e_1, e_1')$$

and

$$\mathcal{A} \vdash_{D} \cup_{E} b \rhd Y_{1}(e'_{1})$$

Furt from t s p rs of frest s t pot s s of to o t n t p rt t on  $B_{ijkl}$  ow or  $b' \in B_{ijkl}$  w

$$I^{b'} = \left\{ (p,q) \mid b' \models \alpha_{ikp} = \beta_{jlq} \ \text{n} \ X_{f(ikp)}(e_{ikp}) \blacktriangleleft^{b'}_L Y_{g(jlq)}(e_{jlq}) \right\}.$$

prop rt s o  $B_{ijkl}$  v n - nsur t t  $I^{b'}$  s tot r n sur t v r r t on on  $P_{ik} \times Q_{jl}$  us t s

so n ppr tono A or I wr v us 
$$\vdash_{D\ \cup E} b'\rhd\beta_{jlq}.Y_{g(jlq)}(e_{jlq})=\alpha_{ikp}.Y_{g(jlq)}(e_{jlq}).$$

rp tt s or q n to o t n q – s qu nt q s r tr s r to st r s us n s q r r q n to w n to t q s built in favour o p n q n q n q n q n q n to o t n q – s qu nt q s r r q n to o t n q – s qu nt q n

 $\mathbf{\hat{b}}_{\mathbf{j}}$   $\mathbf{o}_{\mathbf{j}}$  (Completeness) Let t and u be regular terms with identifiers in D, where D is a regular, guarded, declaration. Then

$$t \bowtie_L^b u \text{ implies } \mathcal{A} \vdash_D b \rhd t = u.$$

rst tr ns of t n u nto r r t ons us n ropos t on 0 --- s r s r r t ons  $D_A = \{X_i\}$  n  $D = \{Y_j\}$  su t t

$$\vdash_{D \cup D_1} \quad \triangleright t = X_1(x) \quad \text{n} \quad \vdash_{D \cup D} \quad \triangleright u = Y_1(y)$$

w r fv(t) = x n fv(u) = y or ov r w s ont p r t rs now t t  $X_1$  s of t t  $D_1$  n D r st n r of s n

• w n v r  $p \xrightarrow{\alpha} p'$   $\alpha \neq c$  t n  $q \Longrightarrow q'$  or so q' su t t  $(p',q') \in \mathcal{R}$ 

wts tron tons or q - wrt  $p \approx_L q$  tr sts rtw surton  $\mathcal{R}$  su t t $(p,q) \in \mathcal{R}$  – wr ropt susrptL untrw susst or spon n early quvrn – Lat obs rvat on con runc or v runp ss n CC  $\stackrel{\text{def}}{=}$  st r r t on n  $p \stackrel{\text{def}}{=} q$ 

- w n v r  $p \xrightarrow{c} (x)t$  t n  $q \Longrightarrow (y)u$  or so (y)u su t t or  $v \in Val$  t r s q'su t  $t u[v/y] \stackrel{\varepsilon}{\Longrightarrow} q'$  n  $t[v/x] \approx q'$
- w n v r  $p \xrightarrow{\alpha} p' \alpha \neq c$  t n  $q \Longrightarrow q'$  or so q' su t t  $p' \approx q'$

ron w t t s  $\blacksquare$  on tons on q-

Etnsvus os vor svnt s or vru pssn CC wr us ort r n ro ts ptr-usw nrtws for sturtons nrts for on run or t srnu –

s  $\blacksquare$  or v rs on o t w transton r r t on  $\Longrightarrow$  s n s or rows

- $t \stackrel{,\varepsilon}{\Longrightarrow} t$
- $t \stackrel{b,\alpha}{\longmapsto} u$  pr  $s t \stackrel{b,\alpha}{\Longrightarrow} u$
- $\bullet \ t \xrightarrow{b,\tau} \stackrel{b',\alpha}{\Longrightarrow} u \quad \text{pr} \quad s \ t \xrightarrow{b \land b',\alpha} u$
- $t \stackrel{b,\tau}{\Longrightarrow} \stackrel{b',\tau}{\Longrightarrow} u \quad \text{pr} \quad s \quad t \stackrel{b \wedge b',\tau}{\Longrightarrow} u$
- $\bullet t \xrightarrow{b,c} \xrightarrow{b',\tau} u \qquad \text{pr s } t \xrightarrow{b \wedge b',c} \xrightarrow{e} u$

uppos  $= \{S^b\}$  s oor n n  $\mathbf{F}$  r o r r t ons $-\mathbf{D}$  n  $\mathcal{WSB}(\ )$  to  $\mathbf{t}$ orrtons su t t

 $(t,u) \in \mathcal{WSB}(\ )^b$  w n v r  $t \stackrel{b_{\cdot l} \cdot \alpha}{\longrightarrow} t'$  t r sts v r r z su t t z  $\not\in fv(b,t,u)$  n  $b \wedge b_1$  prtton B su or  $b' \in B$   $z \notin fv(b')$  nt r sts  $u \stackrel{b}{\Longrightarrow} a'$  su t t  $b' \models b$ 

- $\alpha$  s  $\tau$  t n  $\beta \equiv \tau$  n  $(t', u') \in S^{b'}$
- $\cdot$   $\alpha$  s c e t n  $\beta \equiv c$  e' w t  $b' \models e = e'$  n  $(t', u') \in S^{b'}$
- $\cdot$   $\alpha$  s c x t  $n\beta \equiv c$  y or so  $\beta$  y n t r sts b' p r t t or  $\beta$  $b'' \in B'$ t r s u'' su t  $tu'[z/y] \stackrel{b',\varepsilon}{\Longrightarrow} u''$  w t  $b'' \models b'$  n  $(t'[z/x], u'') \in S^{b''}$

 $rrr \{S^b\}$  at wa sy bo cbs uaton  $S^b \subseteq \mathcal{WSB}(\ )^b$  or b n not t r st su  $\{ \approx^b \}$  -  $\bullet$  n n w now us t n t on o  $\approx^b$  to n  $\stackrel{\text{def}}{=}$  t r r st on run ont n  $n \approx^b$ 

 $t \stackrel{\text{def}}{=} u$  w n v r  $t \stackrel{b_{\perp} \alpha}{\longmapsto} t'$  t r sts v r r z su t t z  $\notin fv(b,t,u)$  n  $b \wedge b_1$  p rt t on B su t t or  $b' \in B$   $z \notin fv(b')$  n t r sts  $u \stackrel{b}{\Longrightarrow} u'$ 

p Suppose we have standard, saturated declarations

$$X_i \Leftarrow= \lambda x_i. \sum_{k \in K_i} c_{ik} \rightarrow \sum_{p \in P_{ik}} \alpha_{ikp}. X_{f(ikp)}(e_{ikp})$$

and

$$Y_j \Longleftrightarrow \lambda y_j. \sum_{l \in L_j} d_{jl} 
ightarrow \sum_{q \in \mathcal{Q}_{jl}} eta_{jlq}. X_{g(jlq)}(e_{jlq}).$$

Also suppose that  $X_i(x_i) \approx^{b \wedge c_{ik} \wedge d_{jl}} Y_i(y_i)$ , then  $t_{ik} \approx^{b \wedge c_{ik} \wedge d_{jl}} u_{il}$  where

$$t_{ik} \equiv \sum_{P_{ik}} \alpha_{ikp}.X_{f(ikp)}(e_{ikp})$$

and

$$u_{jl} \equiv \sum_{Q_{jl}} \beta_{jlq} . Y_{g(jlq)}(e_{jlq}).$$

Moreover there exist disjoint  $b \wedge c_{ik} \wedge d_{jl}$ -partitions  $B_{ijkl}^c, B_{ijkl}^c$  and  $B_{ijkl}^{\tau}$  such that

- For each  $b' \in B^c_{ijkl}$  and for each  $p \in P_{ik}$  such that  $\alpha_{ikp} \equiv c$  e, there exists a  $q \in Q_{jl}$  such that  $\beta_{ilq} \equiv c \ e' \ with \ b' \models e = e' \ and \ X_{f(ikp)}(e_{ikp}) \approx^{b'} Y_{g(ilq)}(e_{ilq}).$
- For each  $b' \in B_{ijkl}^{\tau}$  and for each  $p \in P_{ik}$  such that  $\alpha_{ikp} \equiv \tau$ , then either  $X_{f(ikp)}(e_{ikp}) \approx^{b'} Y_i(y_j)$ or there exists a  $q \in Q_{il}$  such that  $\beta_{ilq} \equiv \tau$  with  $X_{f(ikp)}(e_{ikp}) \approx^{b'} Y_{g(ilq)}(e_{ilq})$
- For each  $b' \in B^c_{ikjl}$  and for each  $p \in P_{ik}$  such that  $\alpha_{ikp} \equiv c$  w, there exists a  $q \in Q_{jl}$  such that  $\beta_{jlq} \equiv c$  w and there exists a disjoint b'-partition,  $B'_{p,b'}$  such that for each  $b'' \in B'_{p,b'}$  we have  $X_{f(ikp)}(e_{ikp}) \approx^{b''} Y_{g(jlq)}(e_{jlq}) \text{ or } Y_{g(jlq)}(e_{jlq}) \xrightarrow{d,\tau} Y_{j(b'')}(e(b'')) \text{ for some } j(b'') \text{ and } e(b'') \text{ with } b'' \models d \text{ and } X_{f(ikp)}(e_{ikp}) \approx^{b''} Y_{j(b'')}(e(b''))$

(Similar conditions for each  $q \in Q_{il}$  follow by symmetry).

where t is a new part  $b_{ijkl}$  so near new part  $b_{ijkl}$  so new part  $b_{ijkl$ 

$$\mathbf{C} \quad \text{now t} \quad \mathsf{t} \ X_i(x_i) \approx^{b_{ijkl}} Y_j(y_j) \quad \mathsf{n} \quad \mathsf{t} \quad \mathsf{t} \ X_i(x_i) \stackrel{c_{ij}, c}{\rightleftharpoons} \stackrel{e}{\mathbb{M}}$$

From  $\{q_1,\ldots,q_m\}$  state  $mq\in Q_{jl}$  suit t  $\beta_{jlq}$  so to c e t n with c

$$E^c = \left\{ \bigwedge_{1 \leq i \leq m} b_i \mid b_i \in B^c_{q_i}, 1 \leq i \leq m \right\}.$$

prtton $B^c_{ijkl}$  wront nonuntonso oor nsonprws roll  $D^c$  n $E^c$  – For m tss

$$B_{ijkl}^c = \left\{ b \wedge b' \mid b \in D^c, b' \in E^c \right\}.$$

It s so prove that to tenderal tendera so  $b_p \in B_p^c$  n t t  $b_p$  s urt r p rt t on nto  $B'_{p,b_p}$ tu m n b' p rt t on m $B'_{p,b'}$  r utt s sot n s pr n  $\left\{b'' \wedge b' \mid b'' \in B'_{p,b_{PSI}}\right\}$ 

s ow n **r**t rt OPTOWS

 $\mathbf{v}_{j}$   $\mathbf{o}_{j}$  Let  $D_{1} = \{X_{i} \Leftarrow g_{i}\}_{I}$  and  $D_{i} = \{Y_{j} \Leftarrow g_{j}\}_{J}$  be standard, saturated, strongly guarded declarations such that  $X_{1}$  does not appear in any  $g_{i}$  and  $Y_{1}$  does not appear in any  $g_{j}$ . If  $X_{\mathbf{l}}(e_{\mathbf{l}}) \triangleq^b Y_{\mathbf{l}}(e'_{\mathbf{l}})$  then there exists a standard declaration  $E = \{Z_{ij} \longleftarrow h_{ij}\}_{I \times I}$ 

$$I_{b'}^c = \left\{ \right.$$

rstst por s us  $p \in P_{ik}$  su t t $lpha_{ikp}$  ssol c e ppor sn $I_{b'}^c$  ightharpoonup r rr, w now oos n r tr r  $b' \in B^c$ 

n us 
$$T$$
 to o t  $\mathfrak{g}$  or  $b'$ 

$$\vdash b' \triangleright c \ w.X_{\varepsilon(:i,n)}(e_{ikn}) \equiv c \ w.X_{\varepsilon(:i,n)}(e_{ikn}) + c \ w. \quad \sum \quad b'' \rightarrow X_{\varepsilon(:kn)}(e_{ikn})$$

$$\vdash b' \rhd c \ w.X_{f(ikp)}(e_{ikp}) = c \ w.X_{f(ikp)}(e_{ikp}) + c \ w.\sum_{b'' \in B'_{q,b'}} b'' \to X_{i(b'')}(e(b''))$$

w n nt r sto 
$$t^c$$
 n us n  $-1$  v s us 
$$\vdash b' \rhd t^c = t^c + V[f/Z].$$

$$\begin{split} \vdash b' \rhd V^c_{ijkl}[f/Z] &= V_{1}[f/Z] + V\ [f/Z] \\ &= t^c \ + V\ [f/Z] \\ &= t^c \end{split}$$

$$\vdash b' \rhd V_{ijkl}^{ au}[f/Z] = t^{ au} + \sum_{\substack{k \in K_i \ b' \in B_{ijkl}^{ au}( au,q) \in I_{b'}^{ au}}} \sum_{b' 
ightarrow au. X_i}$$

- $\cdot \quad \alpha \quad \mathbf{s} \, \tau \, \mathbf{t} \quad \mathbf{n} \, \beta \equiv \tau \quad \mathbf{n} \quad t' \approx^{b'} u'$
- $\cdot$   $\alpha$  s c e t n  $\beta \equiv c$  e' w t  $b' \models e = e'$  n  $t' \approx^{b'} u'$
- $\cdot$   $\alpha$  s c x t n  $\beta \equiv c$  y or so y n  $t'[z/x] \approx^{b'} u'[z/y] -$

r ro ours s tr on tons on ur qur nt ov nsurprs nr t on n s to t proos s t w r n t ons-

v t s orrstr ton

$$\begin{array}{rcl} \ \, \backslash c & = & . \\ (X+Y)\backslash c & = & X\backslash c + Y\backslash c \\ (b\to \alpha.X)\backslash c & = & \left\{\begin{array}{cc} . & \alpha & \text{s } c \text{ } e \text{ } \text{or } c \text{ } x \end{array}\right. \end{array}$$

$$\begin{array}{llll} \text{G v n} & \text{r r t on } D = \left\{ X_i \Longleftarrow \lambda x_i. \sum\limits_{k \in K_i} \alpha_{ik}. X_{f(ik)}(e_{ik}) \right\}_I \text{t n w n n t } regular \\ \text{r r t on } D \backslash c & \text{s} & \\ & \left\{ Z_i \Longleftarrow \lambda x_i. \sum\limits_{\alpha_{ik} \neq c \ , c} \alpha_{ik}. Z_{f(ik)}(e_{ik}) \right\}_I . \end{array}$$

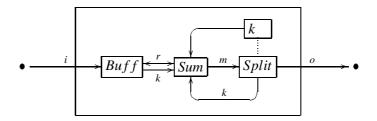


Figure 6.4. Ppr nt tono Spec

$$p \equiv X_i(e)$$
 n  $q \equiv C_i'[e/x_i]$  uppos t t  $p \xrightarrow{\alpha} p'$  or so  $p'$  so t t  $[b_{ik}[e/x_i]] =$  or so  $k \in K_i$  w t  $\alpha = \alpha_{ik}[e/x_i]$  n  $p' \equiv X_{f(ik)}(e_{ik}[e/x_i])$  now t t

$$q \xrightarrow{\tau} C_i''[e/x_i] \xrightarrow{\tau} C_i[e/x_i] \xrightarrow{\alpha} q'$$

$$\mathbf{w} \quad \mathbf{r} \quad q' \equiv C'_{f(ik)}[e$$

Chapter 6. Unique Fixpoint Induction

**G p**//

.-

s ns, s ts o on r t v rus n s n s str t v rus — r n n ppro r s n t nt rpr t t on o t un t ons n t t s n tur — ur ppro rows or n o precise nt rpr t t on on nt rpr t t on o un t ons s t in n t str t on on v rus — o t str t n n  $f_A$  o un t on f o r t on, s n s

$$f_A(V) = \{ f(v) \mid v \in V \}$$

w r V n n str t v ru s s to on r t v ru s row Val us w r un r to r p so o t n tso n r r str t on—For V pr w w s to V on str t ro r o t pro ss p(x) w r

$$p \Leftarrow= \lambda y.c \ y.p(y+1)$$

t nt s or s nt s nu s abstract values on s r n t on r t v r u s t t x t - In t m, x our n v r u, w w r pr s nt t s t Val - s on output row p(x)

nt r.s o nst nt t t r nt v ru t r un or n – For pr t pro ss

$$X \iff \lambda x.(X(x+1)+a x.),$$

w n nst nt t t s n n n t r r n n s or r p - Gur r urs ons r w s v n t r r n n s or r p s so t s r r t t X nnot r u to u r r t on- wo t ppro s spr n to

## B o, p

- 1 -A r-Non-well-founded Sets, vorum 140 CSLI Lecture Notes— t n or n v rs t, 1 p
- I A on -D owr vortor of psort  $\pi$  rurus—In Proc.

- E-Br nt-Gr p s rort s or oor n un ton n pur ton-IEEE Transactions on Computers, C 1 Au ust 1 p

- A-Gor on- Functional Programming and Input/Output- D st n u s ss rt t ons n oput rs n -C r n v rs t r ss 1 4 p

  1 A-Gor on-B s r t s t or o un ton pro r n n ours B-C

  B-C D p rt nto Co put r n A r us n v rs t 1 p
- J-F-Groot H- STATE STATE

- C-A-r tr Con urr n t or In -Br u r s n G-v n r tors Advances in Petri Nets 1986, Part I, Petri Nets: Central Models and Their Properties vorus 40 Lecture Notes in Computer Science p s 4 4 pr n r r 1 p.1
- I 4 A-nur-n rn rn n strutur snt sint snro sor tv s st s-In rr Brur tor Proceedings 12th ICALP, pronvorus 1 40 Lecture Notes

```
barb r s wrt on or CB 4

barb r on run or CB 4

s wrt on qu v r n

s see su st tut on s tur t

on r t on qu v r n

TD t is so v r r r t on D

L r s wrt on qu v r n

L r t s wrt on qu v r n

b r s or s wrt on

L r t s wrt on qu v r n

b r t s wrt on qu v r n

b r t s wrt on qu v r n

b r t s wrt on qu v r n

b r t s wrt on qu v r n
```

